

Even HW answers

72.  $f^{-1}(x) = 4(x-7)$

74.  $f^{-1}(x) = (x+5)^3$

76.  $f^{-1}(x) = x^{-1}$

**INVERSE  
FUNCTIONS!**

HORIZONTAL LINE TEST:  
if a function passes the  
test, then **the inverse is  
also a function!**

**Terminology:** A function whose inverse is also a function is called "**one - to - one**"

[in other words, a function which passes the horizontal line test is "one to one"]

If  $f$  is a one-to-one function,  
then we write the inverse function  $f^{-1}$

The -1 in  $f^{-1}$  is not  
an exponent

THEOREM:

$$f^{-1}(f(x)) =$$

$$f(f^{-1}(x)) =$$

$$f(x) = 2x^3 + 1$$

$$f^{-1}(x) = \sqrt[3]{\frac{x-1}{2}}$$

$$f(x) = 2x^3 + 1$$

- (1) cube
- (2) multiply by 2
- (3) add 1

$$f^{-1}(x) = \sqrt[3]{\frac{x-1}{2}}$$

- (1) subtract 1
- (2) divide by 2
- (3) cube root

$$f(x) = x^3 - 2$$

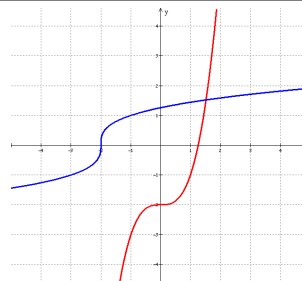
$$f^{-1}(x) = \sqrt[3]{x+2}$$

$$f(f^{-1}(2)) =$$

$$f^{-1}(f(0.5)) =$$

$$f(f^{-1}(-2)) =$$

$$f^{-1}(f(-2)) =$$



By the end of class you should be able to:

1. define an exponential function
2. evaluate exponential functions
3. understand how exponential functions look and translate graphically

**GROUP WORK!**  
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Let's come back together  
and discuss our findings!

So what do you think the maximum number  
of times a piece of paper can be folded?

What about something thinner than paper --  
like foil?

In January 2002, **while a junior in high school**, Gallivan demonstrated that a single piece of toilet paper, 4000 ft (1200 m) in length, can be folded in half **twelve times**.

The previous limit to folding any piece of paper in half had **long been believed to be only eight times**.

She also folded a single square sheet of gold foil in half twelve times. Not only did she provide the empirical proof, but she also derived an equation that yielded the width of paper,  $W$ , needed in order to fold a piece of paper of thickness  $t$  any  $n$  number of times.

Gallivan's story was mentioned in the episode Identity Crisis [1] of Numb3rs on CBS in 2005 and on an episode of MythBusters [2] on The Discovery Channel in 2007.

In May 2007 Britney Gallivan graduated from UC Berkeley with a degree in Environmental Science from the College of Natural Resources.

[wikipedia: [http://en.wikipedia.org/wiki/Britney\\_Gallivan](http://en.wikipedia.org/wiki/Britney_Gallivan)]



